

Exam 1

Friday, February 24

- (20 points) Sketch the graph of a function $f(x)$ with domain $[-3, 2]$ that
 - is continuous at -2 from the positive side but not from the negative side,
 - is discontinuous at 2 ,
 - goes to infinity at 1 ,
 - is continuous everywhere else on its domain, and
 - is not differentiable at 0 .
- (20 points) Evaluate $\lim_{x \rightarrow 0} \frac{1 - \cos x}{x^2}$. Hint: Multiply and divide by $1 + \cos x$.
- (30 points) Let $y = e^{x/\sqrt{2}} \sin \frac{x}{\sqrt{2}}$. Find $\frac{dy}{dx}$, $\frac{d^2y}{dx^2}$, $\frac{d^3y}{dx^3}$, and $\frac{d^4y}{dx^4}$. Hint: Simplify as often as possible. $\frac{d^2y}{dx^2}$ looks a lot like y . $\frac{d^4y}{dx^4}$ looks even more like y .
- (30 points) A light is attached to the wall of a building 64 feet above the ground. A ball is dropped from the same height 20 feet away from the side of the building. How fast is the shadow of the ball moving along the ground after 1 second? Recall that the equation for motion with constant acceleration is $y = \frac{1}{2}at^2 + v_0t + y_0$ and the acceleration due to gravity is -32 ft/s^2 . Hint: Use similar triangles, not sines and cosines.