

1. Write down the formulas for $\mathbf{T}, \mathbf{N}, \mathbf{B}, a_T, a_N, a, \kappa(t)$, speed, and arclength
2. Given $\mathbf{r}(t)$, write:
 - (a) 3 different ways to determine \mathbf{N}
 - (b) 2 different ways to determine a_T
 - (c) 2 different ways to determine a_N
3. Find the arclength of
4. $\mathbf{r}(t) = \langle t^2, -2t^3, 6t^3 \rangle$ for $0 \leq t \leq 1$
5. Find $\kappa, \mathbf{T}, \mathbf{N}, \mathbf{B}$ at the given time
 $\mathbf{r}(t) = \langle \cos^3(t), 0, \sin^3(t) \rangle$, $t = \frac{\pi}{2}$
6. (a) What does $\mathbf{u} \cdot \mathbf{v} = 0$ imply?
 (b) What does $\mathbf{u} \cdot \mathbf{u} = 0$ imply?
 (c) What does $\mathbf{u} \times \mathbf{v} = 0$ imply?
 (d) What is $\mathbf{u} \times \mathbf{u}$?
7. Find the distance between the parallel lines
 $-3x + 2y + z = 9$ and $6x - 4y - 2z = 19$
8. Prove that $\mathbf{u} \cdot \mathbf{v} = \frac{1}{4}|\mathbf{u} + \mathbf{v}|^2 - \frac{1}{4}|\mathbf{u} - \mathbf{v}|^2$
9. Find the equation of the plane passing through $(-1, 2, 3)$ such that:
 - (a) the plane is parallel to the plane $2x + 4y - z = 6$
 - (b) the plane passes through $(0, 1, 0)$ and $(0, 0, 1)$
10. Show that if $\mathbf{a}, \mathbf{b}, \mathbf{c}, \mathbf{d}$ are all in the same plane, then
 $(\mathbf{a} \times \mathbf{b}) \times (\mathbf{c} \times \mathbf{d}) = \mathbf{0}$
11. Find the equation of the plane through $(6, 2, -1)$ that is perpendicular to the line of intersection of the planes
 $4x - 3y + 2z = -5$ and $3x + 2y - z = -11$
12. A bee is flying along a path described by $\mathbf{b}(t) = \langle 2t, \sin t, \cos t + 1 \rangle$, and a fly flies along a path described by $\mathbf{f}(t) = \langle t + k, \sin(2t), \cos(2t) + 1 \rangle$
 Can I choose a $k > 0$ such that the bee and the fly collide? Give a formula for this k if so.
13. Sketch the graph of:
 - (a) $8x^2 + 18y^2 - 2z^2 = 0$
 - (b) $8x^2 + 18y^2 - 2x^2 = 1$

14. Convert $\rho = 2 \cos \phi$ to cylindrical coordinates
15. Write the equation of the paraboloid $(x^2 + y^2 - z = 0)$ in cylindrical and spherical coordinates
16. Find the slope of the tangent line to the curve created by intersection of $2z = \sqrt{9x^2 + 9y^2 - 36}$ with the plane $y = 1$ at $(2, 1, \frac{3}{2})$
17. Find the following limits:
- (a) $\lim_{(x,y) \rightarrow (0,0)} \frac{\tan(x^2+y^2)}{x^2+y^2}$
- (b) $\lim_{(x,y) \rightarrow (0,0)} \frac{\cos(x^2+y^2)}{x^2+y^2}$
18. Find the tangent plane to:
- (a) $2z = \sqrt{9x^2 + 9y^2 - 36}$ at $(2, 1, \frac{3}{2})$
- (b) $z = 10x^2 + 4x + 9y^2 - 6xy + 4$ at $(2, 1, 45)$
19. Find the gradient of
- (a) $f(x, y, z) = xz \ln(x + y + z)$
- (b) $f(x, y, z) = \sin^3(x^2y)$