

1. Do the following book problems (this would have been the homework for the final week)
 Section 17.6 3,7,11
 Section 17.7 3,7,11,19
2. Write the triple integral over S of $f(x, y, z)$ if S is the tetrahedron with vertices $(0, 0, 0)$, $(3, 2, 0)$, $(0, 3, 0)$, $(0, 0, 2)$
3. Find the volume of the solid bounded by the cylinders $x^2 = y$ and $z^2 = y$ and the plane $y = 1$
4. Find $\int \int \int_S xy^2z^3 dx dy dz$ where S is the solid bounded by the surface $z = xy$ and the planes $y = x$, $x = 1$, $z = 0$
5. Find $\int \int \int_S xyz$ where S is the region defined by $x \geq 0$, $y \geq 0$, $z \geq 0$, $x^2 + y^2 + z^2 \leq 1$
6. Assume we have a sphere of radius a , centered at the origin. If we look at a wedge of the sphere defined by the section bounded by the half-planes $\theta = \alpha$ and $\theta = -\alpha$, find the x-coordinate of the center of mass and the average distance from the z-axis
7. Assuming that the required partial derivatives exists and are continuous, show that
 - (a) $\text{div curl } \mathbf{F} = 0$
 - (b) $\text{curl grad } f = \mathbf{0}$
 - (c) $\text{div}(f\mathbf{F}) = (f)(\text{div } \mathbf{F}) + (\text{grad } f) \cdot \mathbf{F}$
 - (d) $\text{curl}(f\mathbf{F}) = (f)(\text{curl } \mathbf{F}) + (\text{grad } f) \times \mathbf{F}$
8. Calculate the line integral of the vector field $\mathbf{F} = (x^2 - 2xy)\mathbf{i} + (y^2 - 2xy)\mathbf{j}$ from $(-1, 1)$ to $(1, 1)$ along the parabola $y = x^2$
9. Calculate the line integral of the vector field $\mathbf{F} = x\mathbf{i} + y\mathbf{j} + (xz - y)\mathbf{k}$ along the curve $\alpha(t) = t^2\mathbf{i} + 2t\mathbf{j} + 4t^3\mathbf{k}$ $0 \leq t \leq 1$
10. Calculate $\int_C y dx + z dy + x dz$ where C is the curve of intersection between the two surfaces $x + y = 2$ and $x^2 + y^2 + z^2 = 2(x + y)$. The curve is traversed once, in a clockwise direction when viewed from the origin.
11. Is \mathbf{F} conservative?
 - (a) $\mathbf{F} = (x, y)$
 - (b) $\mathbf{F} = (\sin y - y \sin x + x, \cos x + x \cos y + y)$
 - (c) $\mathbf{F} = (y^2 \cos x + z^3, 2y \sin x - 4, 3xz^2 + 2)$
 - (d) $\mathbf{F} = (-e^{-x} \ln y, e^{-x} y^{-1})$
12. Evaluate $\int_C \sqrt{y} dx + \sqrt{x} dy$ where C is the closed curve formed by $y = 0$, $x = 2$, and $y = \frac{x^2}{2}$

13. Find the work done by $\mathbf{F} = (x^2 + y^2)\mathbf{i} - 2xy\mathbf{j}$ in moving a body counterclockwise around the unit square with vertices $(0,0)$, $(1,0)$, $(0,1)$, $(1,1)$
14. Evaluate the surface integral $\int \int_G 2y^2 + z dS$ where G is the surface of the cube $0 \leq x \leq 1$, $0 \leq y \leq 1$, $0 \leq z \leq 1$
15. Find the mass of the surface $z = 1 - \frac{1}{2}(x^2 + y^2)$ over $0 \leq x \leq 1$, $0 \leq y \leq 1$, $z = 0$, if $\delta(x, y, z) = kxy$ for some constant k
16. We are looking at a region defined by the top part of the sphere $x^2 + y^2 + z^2 = 25$, cut off by the plane $z = 3$. What is the flux of the vector field $\mathbf{F} = (xz, yz, 1)$
17. Evaluate $\int \int_S \text{curl} \mathbf{F} \cdot \mathbf{n} dS$ where $\mathbf{F} = y^2\mathbf{i} + xy\mathbf{j} + xz\mathbf{k}$ and S is the hemisphere $x^2 + y^2 + z^2 = 1$, $z \geq 0$ with a upward pointing normal component