Let $V$ be a vector space of dimension $n$ over a field $\mathbb{F}$, and let $T : V \to V$ be a linear transformation.

**Definition 1.** The space of alternating $n$-forms on $V$, denoted $\Lambda(V)$, is the (one-dimensional) vector space $\Lambda(V)$ of all $f : V \times \ldots \times V \to \mathbb{F}$ such that $f$ is linear in each variable and 
\[
f(..., v_i, v_{i+1}, ...) = -f(..., v_{i+1}, v_i, ...) \quad \text{for every } 1 \leq i \leq n - 1.
\]

**Definition 2.** We define the determinant of $T$, to be the scalar $\det(T) \in \mathbb{F}$ such that 
\[
f(Tv_1, Tv_2, ..., Tv_n) = \det(T) \cdot f(v_1, v_2, ..., v_n),
\]

for every $f \in \Lambda(V)$, and $v_1, ..., v_n$.

**Definition 3.** For $\lambda \in \mathbb{F}$, the subspace 
\[
V_\lambda = \{ v \in V ; T(v) = \lambda v \},
\]

is called the eigenspace of $T$ associated with $\lambda$.

**IMPORTANT REMARK** In the quiz you will need to repeat exactly what is written here in complete way.

**HW8.** There will be a random question on HW8.

**Good Luck!**